Simulated Data for High Temperature Composite Design

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Abstract

The paper describes an effective formal method that can be used to simulate design properties for composites that is inclusive of all the effects that influence those properties. This effective simulation method is integrated computer codes that include composite micromechanics, composite macromechanics, laminate theory, structural analysis, and multi-factor interaction model. Demonstration of the method includes sample examples for static, thermal, and fracture reliability for a unidirectional metal matrix composite as well as rupture strength and fatigue strength for a high temperature super alloy. Typical results obtained for a unidirectional composite show that the thermal properties are more sensitive to internal local damage, the longitudinal properties degrade slowly with temperature, the transverse and shear properties degrade rapidly with temperature as do rupture strength and fatigue strength for super alloys.

Introduction

As candidate materials for advanced high temperature aerospace structures, metal matrix composites (MMCs) have been the subject of considerable interest and extensive research. With concurrent advances in processing, fabrication, and experimental mechanics, MMCs will increasingly be used as structural materials for advanced propulsion systems. The extreme temperatures and stresses of these propulsion systems create a hostile environment for the composite to withstand. Therefore, the analysis and design of these materials are critically important and require the use of mathematical models to predict thermal and mechanical behavior. One such model is the computer code METCAN (METal matrix Composite ANalyzer, reference 1) developed at NASA Glenn Research Center.

This paper presents the mechanical and thermal properties of a unidirectional composite from silicon carbide (SiC)/titanium (Ti6) MMC as computationally simulated by METCAN from constituents properties as described subsequently. It provides results for one fiber volume ratio at a range of temperatures in graphical form. These plots include stress-strain, elastic and shear moduli, Poisson’s ratio, thermal expansion, and thermal conductivity. Similar information can be readily generated for: 1) other loading condition, 2) other composites, and 3) other service conditions. A list of symbols used is included in the appendix where a short table of conversion factors from customary units to SI units is also included.

Background

METCAN has the capability to predict many aspects of high temperature MMCs by using room temperature constituent properties. METCAN’s integrated approach is illustrated in figure 1 as a cyclic arrangement that defines the computational methodology for each load increment. As can be seen from the figure, this predictive capability consists of several computational modules encompassing the material nonlinear behavior (bottom), composite mechanics (sides), and the finite element analysis of structural components (top). Material nonlinearity is treated at the constituent level, where the current material model, namely the Multi-Factor Interaction Model (MFIM), figure 2, describes a time-temperature-stress
**Figure 1.**—Integrated approach to metal-matrix composite analysis.

\[
\frac{P}{P_0} = \begin{bmatrix} T_F - T \\ T_F - T_0 \end{bmatrix}^n \begin{bmatrix} S_F - \sigma \\ S_F - \sigma_0 \end{bmatrix}^m \begin{bmatrix} S_F - \sigma_s \\ S_F - \sigma_0 \end{bmatrix}^l \begin{bmatrix} T_F - T \\ T_F - T_0 \end{bmatrix}^k \begin{bmatrix} R_F - R \\ R_F - R_0 \end{bmatrix}^p \\
\begin{bmatrix} N_{MF} - N_M \\ N_{MF} - N_{M0} \end{bmatrix}^q \begin{bmatrix} N_{TF} - N_{T} \\ N_{TF} - N_{T0} \end{bmatrix}^r \begin{bmatrix} T_F - T \\ T_F - T_0 \end{bmatrix}^s \]

**Rationale:**
- Gradual effects during most range, rapidly degrading near final stages
- Representative of the in situ behavior for fiber, matrix interphase, coating
- Introduction of primitive variables (PV)
- Consistent in situ representation of all constituent properties in terms of PV
- Room temperature values for reference properties
- Continuous interphase growth
- Simultaneous interaction of all primitive variables
- Adaptability to new materials
- Amenable to verification inclusive of all properties
- Readily adaptable to incremental computational simulation

**Notations:**
- \( P \) - property
- \( T \) - temperature
- \( S \) - strength
- \( R \) - metallurgical reaction
- \( N \) - number of cycles
- \( T \) - time
- Over dot - rate
- Subscripts: 0 - reference; F - final; m - mechanical; t - thermal

**Figure 2.**—Assumed multi-factor interaction relationship to represent the various factors which influence in situ constituent materials behavior.
dependence of a constituent’s mechanical and thermal properties at any point in its material history (ref. 2). Characteristic properties of the composite are calculated from the instantaneous constituent properties using composite mechanics. This synthesis results in a point description of equivalent pseudo-homogeneous properties for the composite.

Naturally, some assumptions have been made in the development of this code. The MFIM utilizes a large number of exponents that, ideally, have been calculated from experimental data. When reliable experimental data is unavailable, default values are used. These values were established from studies conducted on other MMCs (ref. 3). The exponents used in this study are summarized in table 1. Secondly, the Ti6 matrix melting temperature in METCAN was given a value close to the consolidation temperature. Since the matrix has no remaining strength at the consolidation temperature and METCAN must simulate this behavior, the actual melting temperature was replaced with one that was slightly higher than the consolidation temperature. The room temperature constituent properties used are listed in table 2. Verification of METCAN (comparisons with experimental data) is described in reference 4.

Additionally, a modification was made in METCAN for this particular task. Since progressive failure of the composite was not a consideration, the method of stopping the program after failure was altered slightly. Normally, when failure occurs in one region, the load is channeled into the remaining regions until the composite suffers a complete fracture. For this study, once failure takes place in a critical region, the simulation is stopped and the material properties for that strain are set at zero. Under a longitudinal load, this critical region is defined as the fiber. For transverse and shear loads, the determining sector is the micro-region A of the matrix (fig. 2).

### TABLE 1.—METCAN EXPONENTS

<table>
<thead>
<tr>
<th>Exp</th>
<th>Array Location</th>
<th>Property</th>
<th>Determining Property</th>
<th>Values</th>
<th>SiC</th>
<th>Ti6</th>
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<tr>
<td>m</td>
<td>6</td>
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<td>18</td>
<td>CTE</td>
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<td>n</td>
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<td>CTE</td>
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TABLE 2.—INPUT CONSTITUENT PROPERTIES AT ROOM TEMPERATURE

<table>
<thead>
<tr>
<th>Fiber: Silicon Carbide on Aluminum</th>
<th>Matrix: Titanium</th>
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<tr>
<td>Property (units)</td>
<td>Property (units)</td>
</tr>
<tr>
<td>( N_f )</td>
<td>( K_v )</td>
</tr>
<tr>
<td>( D_f )</td>
<td>( \rho_m ) (lb/in**3)</td>
</tr>
<tr>
<td>( \rho_f ) (lb/in**3)</td>
<td>( T_{\text{Min}} ) (F)</td>
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<tr>
<td>( T_{\text{MT}} )</td>
<td>( E_m ) (Mpsi)</td>
</tr>
<tr>
<td>( E_{111} ) (Mpsi)</td>
<td>( \nu_m )</td>
</tr>
<tr>
<td>( E_{222} ) (Mpsi)</td>
<td>( \alpha_m ) (\muin/in/F)</td>
</tr>
<tr>
<td>( G_{122} ) (Mpsi)</td>
<td>( K_m ) (BTU/hr/F/in)</td>
</tr>
<tr>
<td>( G_{233} ) (Mpsi)</td>
<td>( C_m ) (BTU/lb)</td>
</tr>
<tr>
<td>( \nu_{12} )</td>
<td>( S_{\text{MT}} ) (ksi)</td>
</tr>
<tr>
<td>( \nu_{23} )</td>
<td>( S_{\text{MC}} ) (ksi)</td>
</tr>
<tr>
<td>( \alpha_{111} ) (\muin/in/F)</td>
<td>( S_{\text{MS}} ) (ksi)</td>
</tr>
<tr>
<td>( \alpha_{222} ) (\muin/in/F)</td>
<td>( \varepsilon_{\text{MT}} ) (in/in)</td>
</tr>
<tr>
<td>( K_{111} ) (BTU/hr/F/in)</td>
<td>( \varepsilon_{\text{MS}} ) (in/in)</td>
</tr>
<tr>
<td>( K_{222} ) (BTU/hr/F/in)</td>
<td>( \varepsilon_{\text{MC}} ) (in/in)</td>
</tr>
<tr>
<td>( C_f ) (BTU/lb)</td>
<td>( \varepsilon_{\text{MTOR}} ) (in/in)</td>
</tr>
<tr>
<td>( S_{111} ) (ksi)</td>
<td>Processing Temperature</td>
</tr>
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<td>( S_{112} ) (ksi)</td>
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<td>( S_{121} ) (ksi)</td>
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<tr>
<td>( S_{222} ) (ksi)</td>
<td>500</td>
</tr>
<tr>
<td>( S_{223} ) (ksi)</td>
<td>300</td>
</tr>
<tr>
<td>( S_{233} ) (ksi)</td>
<td>300</td>
</tr>
</tbody>
</table>

Results and Significances

For this evaluation, a perfect bond was assumed to exist between the fiber and the matrix. This is reflected by the plots which depict the upper boundaries of the material properties. Fiber volume ratio (FVR) of 0.30 provided a good test for this material. Longitudinal loads were imposed on a unidirectional Silicon Carbide fiber Titanium Matrix (SiC/Ti6) composite system at three different temperatures (70, 500, and 1000 °F) to obtain an extensive profile of the thermal and mechanical properties.

In order to properly model a composite, the residual stresses generated by processing is included. To accomplish this, the cool-down history from consolidation temperature to room temperature (70 °F) was simulated before the mechanical load was applied. For the high temperature cases (500 and 1000 °F), the load was applied after the heat-up from room temperature to service temperature. Due to the mismatch in the coefficient of thermal expansion (CTE), the stresses developed in the fiber were compressive while those developed in the matrix were tensile.

Table 3 presents the anticipated tangent properties of each composite. As predicted by METCAN, each composite’s thermal and mechanical properties were evaluated at the test temperature after a small increment of load was applied. Material properties resulting from a compressive load will vary, but not significantly, from those listed in table 3.
TABLE 3.—ANTICIPATED INITIAL THERMAL AND MECHANICAL PROPERTIES OF A UNIDIRECTIONAL COMPOSITE (0.30 FVR SiC/Ti6)

<table>
<thead>
<tr>
<th>Property</th>
<th>Units</th>
<th>Temperature in °F</th>
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<tbody>
<tr>
<td>α₁₁₁</td>
<td>ppm/F</td>
<td>4.577 4.389 4.205</td>
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<tr>
<td>α₁₂₂</td>
<td>ppm/F</td>
<td>5.571 5.245 5.003</td>
</tr>
<tr>
<td>α₁₃₃</td>
<td>ppm/F</td>
<td>5.571 5.245 5.003</td>
</tr>
<tr>
<td>C₁</td>
<td>BTU/lb</td>
<td>0.157 0.157 0.157</td>
</tr>
<tr>
<td>K₁₁₁</td>
<td>BTU/F-hr*in</td>
<td>0.585 0.619 0.706</td>
</tr>
<tr>
<td>K₁₂₂</td>
<td>BTU/F-hr*in</td>
<td>0.572 0.606 0.701</td>
</tr>
<tr>
<td>K₁₃₃</td>
<td>BTU/F-hr*in</td>
<td>0.572 0.606 0.701</td>
</tr>
<tr>
<td>E₁₁₁</td>
<td>Mpsi</td>
<td>26.676 25.606 23.618</td>
</tr>
<tr>
<td>E₁₂₂</td>
<td>Mpsi</td>
<td>17.884 16.410 13.293</td>
</tr>
<tr>
<td>K₁₃₃</td>
<td>Mpsi</td>
<td>17.884 16.410 13.293</td>
</tr>
<tr>
<td>G₁₁₂</td>
<td>Mpsi</td>
<td>8.373 7.052 5.378</td>
</tr>
<tr>
<td>G₁₂₃</td>
<td>Mpsi</td>
<td>7.227 6.750 5.586</td>
</tr>
<tr>
<td>G₁₁₃</td>
<td>Mpsi</td>
<td>8.373 7.052 5.378</td>
</tr>
<tr>
<td>S₁₁₁T</td>
<td>Ksi</td>
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</tr>
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<td>Ksi</td>
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<td>S₁₂₂T</td>
<td>Ksi</td>
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<td>Ksi</td>
<td>101.75 74.25 45.00</td>
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<tr>
<td>S₁₁₂</td>
<td>Ksi</td>
<td>43.75 36.25 23.75</td>
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<td>Ksi</td>
<td>43.75 36.25 23.75</td>
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<tr>
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<td>Ksi</td>
<td>43.75 36.25 23.75</td>
</tr>
<tr>
<td>ν₁₁₂</td>
<td>in/in</td>
<td>0.255 0.222 0.183</td>
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<td>ν₁₂₃</td>
<td>in/in</td>
<td>0.237 0.215 0.190</td>
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<td>in/in</td>
<td>0.171 0.143 0.103</td>
</tr>
<tr>
<td>ρ₂</td>
<td>lb/in**3</td>
<td>0.152 0.152 0.152</td>
</tr>
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</table>

Note: Properties obtained under initial tensile load. Strengths obtained from respective stress/strain curves.

The plots presented in figures 3 to 10 demonstrate METCAN’s ability to capture the behavior of a metal matrix composite at varying temperatures for one fiber volume ratio. By using these plots as an initial guideline, it becomes clear that the behavior at various fiber volume ratios for different composites can be similarly simulated. It should also become clear that obtaining all this information by test will be time and cost prohibitive.

All the properties in figures 3 to 10 are plotted against longitudinal strain for commonality. The stress strain curve is plotted in figure 3. Note the mild nonlinearity for almost the entire range. Note also the decrease with temperature. The longitudinal modulus is plotted in figure 4. The discontinuities indicate local region (sector A in fig. 2) fractures. It is important to note these discontinuities are imperceptible in the stress-strain plots in figure 3. As can be seen, the modulus decreases continuously and exhibits an abrupt drop near composite fracture which occurs as a result of fiber fractures.
A comparable plot for the transverse modulus is shown in figure 5. Note the insensitivity of the transverse modulus with respect to longitudinal strain. The interpretation for this is that transverse local damage (cracks) has negligible effect on the transverse modulus when a unidirectional composite is loaded along the longitudinal (fiber) direction. Similarly for the in-plane shear modulus, $G_{12}$ plotted versus longitudinal strain $\epsilon_{L11}$ in figure 6. However, this is not the case when the composite is loaded in the transverse or in-plane shear.
The in-plane major Poisson’s ratio \( \nu_{12} \) is plotted versus \( \varepsilon_{11} \) in figure 7. As can be observed, \( \nu_{12} \) is not sensitive to \( \varepsilon_{11} \) which is comparable to \( E_{22} \) and \( G_{12} \) and for the same reasons that were mentioned. A different situation arises when the through-the-thickness \( \nu_{32} \) is plotted versus \( \varepsilon_{11} \). The results are displayed in figure 8. Note that the magnitude increases continuously with discontinuous “jumps” in the region \( 0.3 \leq \varepsilon_{11} \leq 0.5 \). These discontinuous jumps coincide with those in the longitudinal modulus in figure 4. Note also the rapid increase near the fracture region and almost instantaneous drop at fracture.
The reasons for this behavior are the same as previously mentioned. The conclusion from this discussion is that local directional damage may be present that may be detected by some properties and may be insensitive to others. The graphical results described thus far demonstrate that generalizations should be avoided when interpreting test results from these complex composites tested at high temperatures.

Figure 7.—Longitudinal load of SiC/Ti6 at a fiber volume ratio of 0.30: Poisson’s ratio ($v_{L12}$) vs. strain ($\varepsilon_{L11}$) under temperature of 70, 500, and 1000 °F.

Figure 8.—Longitudinal load of SiC/Ti6 at a fiber volume ratio of 0.30: Poisson’s ratio ($v_{L32}$) vs. strain ($\varepsilon_{L11}$) under temperature of 70, 500, and 1000 °F.
The longitudinal thermal expansion coefficient $\alpha_{L11}$ is plotted versus longitudinal strain in figure 9. The curves increase nonlinearly up to the local longitudinal damage exhibited by the instantaneous discontinuity drop. Thereafter remain insensitive till fracture. The important point to be made from the results in figure 9 is that longitudinal thermal expansion monitoring during loading may be a sensitive test to identify local damage in these types of composites. Comparable results for longitudinal thermal conductivity $K_{L11}$ are shown in figure 10. The behavior for $K_{L11}$ is more pronounced than that for $\alpha_{L11}$. However, the interpretation and point to be made are similar to those made for $\alpha_{L11}$.

Time dependent (rupture strength) behavior can be simulated by activating the time factor in the MFIM, which is the last term in the MFIM in figure 2. The combined thermal time effects can be simulated by activating the temperature and time factors (first and last terms, figure 2) simultaneously. The combined results obtained for a monolithic super alloy are shown in figure 11. Also, two experimental available points are plotted for comparison. The important point to be noted is that information for preliminary designs or early assessments can be generated for emerging or projected materials for specific applications. Comparable information can be generated for fatigue endurance. This is obtained by activating the mechanical fatigue factor (sixth term) in the equation in figure 2. These results are plotted in figure 12. Note the relatively rapid drop at small cyclic ratios and the leveling as the cyclic ratio increases. Fatigue resistance for composites has been also evaluated as reported in references 5 and 6. Probabilistic fatigue in composites is described in references 7 and 8.
Figure 10.—Longitudinal load of SiC/Ti6 at a fiber volume ratio of 0.30: thermal conductivity ($K_{L11}$) vs. strain ($\varepsilon_{L11}$) under temperature of 70, 500, and 1000 °F.

Figure 11.—Nickel base alloy B-1900 rupture strength at various temperatures (sustained stress = 90% of static strength).
The major observations from the above discussion are that: (1) The highest laminate strength is along the fiber direction; (2) The room temperature laminate transverse and shear strengths decrease substantially with temperature. The decreases are about 18 percent for the longitudinal tensile strength and about 55 percent for the transverse and shear strengths. Of lesser significance are the observations that: (1) The thermal expansion coefficient and the thermal conductivity indicate abrupt changes in regions where one or both constituents failed. These sharp drops correspond to a somewhat imperceptible change in the slope of the stress-strain plot in figure 3.

Concluding Remarks

The evaluation presents simulated (METCAN generated) results at temperatures of 70, 500, and 1000 °F for SiC/Ti6 at a fiber volume ratio of 0.30. It includes the following: (1) Table of Anticipated Thermal and Mechanical Properties, (2) Stress-Strain Curves, (3) Thermal Conductivities, (4) Thermal Expansions, (5) Elastic and Shear Moduli, and (6) Poisson’s Ratios. It also includes simulated results for stress rupture and fatigue resistance of a high temperature super alloy. It is noted that the method is general and applicable to all types of composites, loading conditions, and service environments.

Some general trends are:

- The highest ultimate tensile strength (UTS) is along the fiber. The room temperature transverse and shear strengths are roughly one third and one fourth, respectively, of the longitudinal UTS. Temperature causes these two strengths to degrade by approximately 55 percent while the longitudinal strength degrades by only 18 percent.
- Some of the curves for the coefficient of thermal expansion (CTE $\alpha$) and thermal conductivity (K) indicate abrupt changes in regions where one or both of the constituents failed. These sharp drops
correspond to a sometimes imperceptible change in the slope of the stress-strain plot. When a failure of this type occurs, the mechanism for heat transfer is disrupted.

- The elastic (E) and shear (G) moduli experience a moderate degradation due to increasing temperature. The highest modulus is along the fiber (26 Mpsi). The transverse moduli are somewhat less (18 Mpsi) while the shear moduli are much smaller (8 Mpsi).
- The major Poisson’s ratio remains about constant as temperature and longitudinal strain increase. The through-the-thickness Poisson’s ratio increases nonlinearly with increasing strain and temperature, which is reflected in the behavior of the corresponding decreases in the longitudinal modulus.
- The rupture strength of a high temperature super alloy decreases rapidly with exposure time and with exposure temperature. The major decrease is from 1500 to 2000 °F because 2000 °F is approaching the melting temperature of the matrix.
- The fatigue strength of the super alloy decreases rapidly at low cyclic ratios and decreases somewhat slower as the cyclic ratio increases.
- The collective results demonstrate the versatility and effectiveness of multi level computational simulation coupled with a multi factor interaction model.

References

Appendix—Symbols List

C = Heat Capacity (BTU/lb)
E = Normal Modulus (Mpsi)
G = Shear Modulus (Mpsi)
K = Thermal Conductivity (BTU/°F*hr*in)
S = Strength (Ksi)
α = Coefficient of Thermal Expansion (ppm/°F)
ε = Strain (in/in %)
ν = Poisson’s Ratio (in/in)
ρ = Density (lb/in³)

Subscripts

ℓ = L Ply Related Quantity
T, C = Tension, Compression
1,2,3 = Material Coordinate System Axes

CONVERSION FACTORS

<table>
<thead>
<tr>
<th>Property</th>
<th>English Units</th>
<th>Multiply By</th>
<th>SI Units</th>
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<tr>
<td>Modulus, (G&amp;E)</td>
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<td>GPa</td>
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<tr>
<td>Strength, (S)</td>
<td>Ksi</td>
<td>6.89</td>
<td>MPa</td>
</tr>
<tr>
<td>Thermal Conductivity, (K)</td>
<td>BTU/°F<em>hr</em>in</td>
<td>6.94</td>
<td>W/m²K</td>
</tr>
<tr>
<td>Heat Capacity, (C)</td>
<td>BTU/lb</td>
<td>2.326</td>
<td>kJ/Kg</td>
</tr>
<tr>
<td>CTE, (α)</td>
<td>ppm/°F</td>
<td>1.8×10⁻⁶</td>
<td>mm/mm K</td>
</tr>
<tr>
<td>Density, (ρ)</td>
<td>lb/in³</td>
<td>27.7</td>
<td>g/cm³</td>
</tr>
</tbody>
</table>
The paper describes an effective formal method that can be used to simulate design properties for composites that is inclusive of all the effects that influence those properties. This effective simulation method is integrated computer codes that include composite micromechanics, composite macromechanics, laminate theory, structural analysis, and multi-factor interaction model. Demonstration of the method includes sample examples for static, thermal, and fracture reliability for a unidirectional metal matrix composite as well as rupture strength and fatigue strength for a high temperature super alloy. Typical results obtained for a unidirectional composite show that the thermal properties are more sensitive to internal local damage, the longitudinal properties degrade slowly with temperature, the transverse and shear properties degrade rapidly with temperature as do rupture strength and fatigue strength for super alloys.